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Vol. XIV.

PART I.

# **JOURNAL**

OF THE

# INSTITUTE OF ACTUARIES

AND

ASSURANCE MAGAZINE.

No. LXIX.

OCTOBER, 1867.

"I hold every man a debtor to his profession, from the which as men of course do seek to receive countenance and profit, so ought they of duty to endeavour themselves by way of amends to be a help and ornament thereunto."—BACON.

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